

Spin-Orbit Twisted Spin Waves: Group Velocity Control

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1 We present a theoretical and experimental study of the interplay between spin-orbit coupling (SOC),
 Coulomb interaction, and motion of conduction electrons in a magnetized two-dimensional electron gas.
 Via a transformation of the many-body Hamiltonian we introduce the concept of spin-orbit twisted spin
2 waves, whose energy dispersions and damping rates are obtained by a simple wave-vector shift of the spin
 waves without SOC. These theoretical predictions are validated by Raman scattering measurements. With
 optical gating of the density, we vary the strength of the SOC to alter the group velocity of the spin wave.
 The findings presented here differ from that of spin systems subject to the Dzyaloshinskii-Moriya
 interaction. Our results pave the way for novel applications in spin-wave routing devices and for the
 realization of lenses for spin waves.

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Spin-wave based transistors are an appealing alternative to
 the traditional charge-based transistor, since spin waves carry
 information with reduced dissipation compared to charge
 currents [1,2]. However, one still has to develop efficient
 methods for controlling the spin waves with low energy cost,
 a condition not satisfied by the manipulation with magnetic
 fields. Spin-orbit coupling (SOC) for conduction electrons is
 a quantum-relativistic interaction emerging for spin-wave
 control [3–9]. An extensive body of literature has been
 devoted to spin waves in ferromagnets subject to the
 Dzyaloshinskii-Moriya interaction (DMI). The DMI arises
 from SOC [10,11] and causes chiral spin-wave dispersions
 [7,12] and damping [13]. In most systems the DMI energy D
 remains an empirical parameter with a magnitude of a few
 percent of the exchange energy J [3,14,15].

The DMI is perfectly suited for spins strongly or weakly
 localized. However, for delocalized spins in a Galilean
 invariant system, for which the kinetic energy interplays
 with the Coulomb exchange and the SOC, all three protagon-
 ists are responsible for the spin-wave dynamics, like in a
 magnetic two-dimensional electron gas (2DEG). One thus
 expects a new type of behavior for the spin waves. In our
 previous works [6,16], we used the concept of a macroscopic
 spin-orbit field enhanced by interactions. Here, by contrast,
 we predict the amplitude and direction of the chiral wave-
 vector shift of spin waves using a transformation of the many-
 body Hamiltonian of a magnetic 2DEG. We introduce the
 concept of spin-orbit twisted spin waves and report con-
 clusive experimental evidence. This leads us to the possibility
 of optically tuning the electron density to modify and even
 reverse the group velocity of the spin waves. We observe
 significant differences between the spin-orbit twisted spin
 waves and the DMI spin waves. Thus, in delocalized spin

systems, our findings show that SOC offers the opportunity to
 control both the direction and velocity of spin waves without
 affecting the spin-wave stiffness and the damping rate.

Spin waves in a magnetic 2DEG.—We focus on spin-
 wave excitations of a magnetic 2DEG embedded in a doped
 Cd_{1-x}Mn_xTe quantum well containing a fraction $x = 0.013$
 of substitutional Mn impurities. This system is ideal to
 study spin excitations of itinerant two-dimensional elec-
 trons, because of its simple free-electronlike conduction
 band. The application of a moderate magnetic field \mathbf{B} (of
 order 2 T) parallel to the plane of the quantum well
 polarizes the spins localized on the randomly distributed
 Mn atoms, which in turn polarizes the electron gas through
 exchange interaction [17]. This causes a Zeeman splitting Z
 of order meV of the electronic states in the conduction band
 [18], with a negligible orbital quantization. One thus
 obtains a spin-polarized 2DEG, with two spin-split para-
 bolic sub-bands. The 2DEG electron density (the number of
 electrons per unit area) is $n_{2D} = 2.7 \times 10^{11} \text{ cm}^{-2}$ and the
 mobility is $1.7 \times 10^5 \text{ cm}^2/\text{Vs}$.

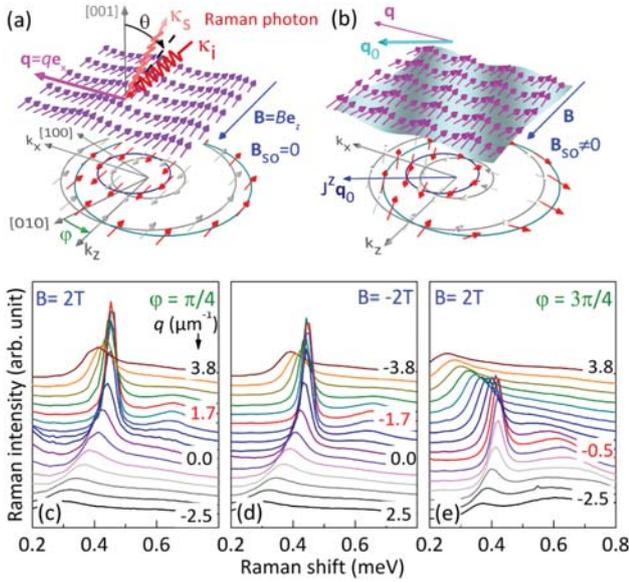
Such a 2DEG supports spin-wave modes located in the
 energy gap below the continuum of single-particle excita-
 tions, the paramagnet equivalent of the Stoner continuum
 [29–31]. The energy dispersion of these spin waves is
 quadratic with the in-plane momentum \mathbf{q} [31–33],

$$\hbar\omega_{\text{sw}}(\mathbf{q}) = Z + S_{\text{sw}} \frac{\hbar^2}{2m^*} q^2 + i\eta_q. \quad (1)$$

Here, $\omega_{\text{sw}}(\mathbf{q})$ is the spin-wave angular frequency, S_{sw} is the
 spin-wave stiffness in units of $\hbar^2/2m^*$, m^* is the electron band
 mass [34], and $\eta_q = \eta_0 + \eta_2 q^2$ is a momentum-dependent

81 damping rate, also quadratic in q , which has an intrinsic part
 82 ($\eta_2 q^2$) caused by a friction with multiple single-particle
 83 excitations [35,36] as experimentally shown [32] and a sample
 84 dependent part (η_0) dominated by magnetic disorder [32]. In
 85 contrast with magnons in ferromagnets, S_{sw} is here a negative
 86 number; i.e., the spin-wave energy starts at the bare Zeeman
 87 energy Z and then decreases, until it merges with the single-
 88 particle continuum where Landau damping occurs.

89 *Spin-orbit twisted spin waves.*—A 2DEG electron occu-
 90 pying the quantum state $|\mathbf{k}\rangle$ is subject to a \mathbf{k} -dependent
 91 spin-orbit magnetic field $\mathbf{B}_{\text{so}}(\mathbf{k})$ [see Fig. 1(b)]. Hence, one
 92 might expect that the spin-wave dynamics (stiffness and
 93 damping) should be affected by the set of individual SO
 94 fields. However, we show that the collective behavior is



F1:1 FIG. 1. (a) Top plane: Raman incoming (κ_i) and outgoing (κ_s)
 F1:2 photon wave vectors. \mathbf{q} is the in-plane momentum of the spin
 F1:3 wave probed by the Raman process. The amplitude and direction
 F1:4 of \mathbf{q} are controlled by θ and φ , respectively. The magnetic field,
 F1:5 parallel to \mathbf{e}_z , is always perpendicular to \mathbf{q} . Bottom plane: the
 F1:6 spin-wave oscillation in real space is associated with an out-of-
 F1:7 phase oscillation of the two Fermi disks in momentum space with
 F1:8 respect to their equilibrium positions (gray circles). Electron
 F1:9 spins remain parallel or antiparallel to \mathbf{B} . (b) Illustration of the
 F1:10 spin-wave twisting caused by SOC. Bottom plane: the momen-
 F1:11 tum-space motion twists the spins with respect to their equi-
 F1:12 librium positions (gray vectors). A z -spin current parallel to \mathbf{q}_0
 F1:13 appears. Top plane: the spins now evolve in a moving wavelike
 F1:14 reference frame (highlighted by the blue shading). Consequently,
 F1:15 the spin waves are twisted with a phase $\mathbf{q}_0 \cdot \mathbf{r}$ (see text). [(c)–(e)]
 F1:16 Electronic Raman spectra obtained by varying the momentum \mathbf{q}
 F1:17 for [(c) and (d)] $\varphi = \pi/4$, $B = \pm 2$ T, and (e) $\varphi = 3\pi/4$,
 F1:18 $B = 2$ T. The low-energy Raman line, sharply peaked, is a
 F1:19 signature of the spin wave. The smoother structure at higher
 F1:20 energy is due to single-particle excitations. The spectrum high-
 F1:21 lighted in red for each case shows the spin-wave maximum
 F1:22 energy.

95 influenced in a rather simple way as a consequence of
 96 symmetries embedded in the SOC.

97 The Hamiltonian of our 2DEG has two parts:
 98 $\hat{H} = \hat{H}_0 + \hat{H}_{\text{SO}}$. \hat{H}_0 describes a translationally invariant
 99 interacting 2DEG subject to a constant magnetic field
 100 applied in the plane of the quantum well and without
 101 Landau orbital quantization [18,31]. The Coulomb inter-
 102 action in \hat{H}_0 leads to the formation of spin waves [31],
 103 which propagate with the dispersion of Eq. (1). \hat{H}_{SO} is the
 104 Hamiltonian due to SOC in the conduction band: $\hat{H}_{\text{SO}} =$
 105 $\sum_i \mathbf{B}_{\text{so}}(\mathbf{k}_i) \cdot \hat{\sigma}_i$ couples the in-plane component of the i th
 106 electronic spin $\hat{\sigma}_i$ with its momentum \mathbf{k}_i .

107 SOC arises from two broken inversion symmetries of the
 108 quantum well [37]: the Rashba contribution [38], of
 109 strength α , due to the asymmetric doping along the growth
 110 direction [001], and the Dresselhaus contribution [39], of
 111 strength β , due to the asymmetry of the CdTe crystalline
 112 unit cell. The Rashba part in $\mathbf{B}_{\text{so}}(\mathbf{k})$ lies in the 2DEG plane
 113 perpendicular to the electron momentum \mathbf{k} ; the
 114 Dresselhaus part has mirror symmetry with respect to
 115 the crystalline axis [100]. The resulting SOC field is
 116 given by

$$\mathbf{B}_{\text{so}}(\mathbf{k}) = \alpha \mathbf{k} \times \mathbf{w} + \beta [(\mathbf{k} \cdot \mathbf{u})\mathbf{u} - (\mathbf{k} \cdot \mathbf{v})\mathbf{v}], \quad (2)$$

117 where the unit vectors \mathbf{u} , \mathbf{v} , and \mathbf{w} are along the crystallo-
 118 graphic directions [100], [010], and [001].

119 When expressing \hat{H}_{SO} in the in-plane coordinates (x, z) ,
 120 where $\mathbf{B} = B\mathbf{e}_z$ and $\mathbf{q} = q\mathbf{e}_x$, as sketched in Fig. 1(a), we
 121 find, to linear order in \mathbf{k} , $\hat{H}_{\text{SO}} = -\hbar \mathbf{q}_0 \cdot \hat{\mathbf{J}}^z + \hbar \mathbf{q}_1 \cdot \hat{\mathbf{J}}^x$.
 122 Here, $\hat{\mathbf{J}}^\nu = (1/2m^*) \sum_i \hat{\mathbf{p}}_i \hat{\sigma}_{\nu,i}$ is the homogenous spin
 123 current of the ν -spin component. The change of coordinates
 124 naturally introduces the two wave vectors \mathbf{q}_0 and \mathbf{q}_1 , where

$$\mathbf{q}_{\{\}} = (2m^*/\hbar^2)[(\alpha \pm \beta \sin 2\varphi)\mathbf{e}_{\{\}} + \beta \cos 2\varphi \mathbf{e}_{\{\}}]. \quad (3)$$

125 Note, first, that the second term in \hat{H}_{SO} couples to the
 126 transverse spin components and thus only produces energy
 127 corrections to second order in SOC [18]. We therefore
 128 neglect it as we limit ourselves to first order considerations.
 129 By contrast, the first term in \hat{H}_{SO} couples to the longi-
 130 tudinal spin components $\hat{\sigma}_{z,i}$. Its effect can be similar to a
 131 magnetic field along z , but activated by the electron motion
 132 embedded in the spin-wave oscillation. We can thus infer
 133 that its strength is periodic in real space: the spin wave
 134 creates a \mathbf{q} periodicity of the spin phases resulting in a
 135 \mathbf{q} periodicity of $\hat{\mathbf{J}}^z$, which in turn twists the spins periodically
 136 in the direction of \mathbf{q}_0 . A positive feedback occurs, leading
 137 to the simple addition of spatial phase changes $\mathbf{q} + \mathbf{q}_0$ in
 138 the spin-wave dispersions as depicted in Fig. 1(b).
 139

140 We can rigorously demonstrate this “spin-orbit twist”
 141 effect by a gauge transformation of \hat{H} with the twist
 142 operator $\hat{U} = e^{-i \sum_i \mathbf{q}_0 \cdot \mathbf{r}_i \hat{\sigma}_{z,i}/2}$ [40]. This transforms the
 143 momentum operator of the i th electron into

144 $\hat{U}\hat{\mathbf{p}}_i\hat{U}^\dagger = \hat{\mathbf{p}}_i + \hbar\mathbf{q}_0\hat{\sigma}_{z,i}/2$, and \hat{H} becomes $\hat{U}\hat{H}\hat{U}^\dagger = \hat{H}_0$,
 145 where we neglected terms in the second order of the SOC
 146 [18]. Hence, the twist operator restores the spin-rotational
 147 invariance [41,42]. \hat{U} imprints a spin rotation along z with a
 148 spatially dependent angle that grows at a rate q_0 along the
 149 \mathbf{q}_0 direction. Consequently, the spin-wave operator is
 150 transformed into $\hat{U}\hat{S}_{+\mathbf{q}}\hat{U}^\dagger = \hat{S}_{+\mathbf{q}+\mathbf{q}_0}$.

151 The final result is that, to first order in SOC, the spin-
 152 wave operators are unchanged, apart from shifting the spin-
 153 wave momentum by \mathbf{q}_0 . The spin-wave equation of motion
 154 in the presence of SOC reads

$$i\hbar\frac{d}{dt}\hat{S}_{+\mathbf{q}} = [\hat{S}_{+\mathbf{q}}, \hat{H}] = \hat{U}^\dagger[\hat{S}_{+\mathbf{q}+\mathbf{q}_0}, \hat{H}_0]\hat{U}. \quad (4)$$

155 This equation leads to a spin-wave dispersion and damping
 156 shifted by a wave vector $-\mathbf{q}_0$, while protecting the spin-
 157 wave stiffness that remains unaffected by SOC,

$$\hbar\omega_{\text{sw}}^{\text{SO}}(\mathbf{q}) = Z + S_{\text{sw}}\frac{\hbar^2}{2m^*}|\mathbf{q} + \mathbf{q}_0|^2 + i\eta_{\mathbf{q}+\mathbf{q}_0}. \quad (5)$$

158 Equations (4) and (5) can be interpreted as follows: the
 159 gauge transformation performed above is equivalent to a
 160 quantum change of reference frame in the spin space, the
 161 latter depending on instantaneous positions of electrons.
 162 The new reference frame for the spins is then moving,
 163 following the electron oscillation in real space [see Fig. 1
 164 (b)]. In this new spin frame, the spin wave experiences a
 165 constant and uniform magnetic field: its propagation is
 166 determined by \hat{H}_0 only. This effect is similar to the drag
 167 of optical or acoustic waves in a moving medium [43,44],
 168 except that here the moving medium refers to the spin
 169 space.

171 *Spin-orbit twist effect evidenced by Raman spectra.*—To
 172 measure the spin-wave dispersions of Eq. (5) we employ
 173 electronic Raman scattering, which transfers a well-controlled
 174 momentum $\mathbf{q} = \mathbf{\kappa}_{i,\parallel} - \mathbf{\kappa}_{s,\parallel} \approx 2\kappa_i \sin\theta\mathbf{e}_x$ to the spin
 175 excitations, where $\mathbf{\kappa}_i$ and $\mathbf{\kappa}_s$ are the momenta of the linearly
 176 cross-polarized incoming and scattered photons, respectively.
 177 The experimental geometry shown in Fig. 1(a)
 178 defines the incidence angle θ and the in-plane azimuthal
 179 angle φ , which control the magnitude and direction of \mathbf{q} ,
 180 respectively. The in-plane orientation of the magnetic field
 181 $\mathbf{B} = B\mathbf{e}_z$ is adjusted so that it is always perpendicular to
 182 $\mathbf{q} = q\mathbf{e}_x$. \mathbf{q} and \mathbf{B} are at the angle φ with, respectively,
 183 the [100] and [010] crystalline directions. The accurate φ
 184 control of \mathbf{q} is crucial to evidence the SOC effects on
 185 spin waves.

186 Figures 1(c)–1(e) show a series of electronic Raman
 187 spectra, obtained at fixed $\varphi = \pi/4$ and $B = \pm 2$ T, and for
 188 transferred momenta q between ∓ 2.5 and $\pm 3.8 \mu\text{m}^{-1}$ [the
 189 positive sign is defined by the orientation of \mathbf{q} in Fig. 1(a)].
 190 The most prominent feature in both series of spectra is the
 191 strong spin-wave Raman line. However, in contrast with the

192 spin-wave dispersion relation (1), which is valid without
 193 SOC, we observe that for $\varphi = \pi/4$ and $B = +2$ T, the
 194 highest spin-wave energy and the minimum linewidth are
 195 not at $q = 0$, but shifted to $q = q_s \approx 1.7 \mu\text{m}^{-1}$ (see the red
 196 spectrum). When inverting B to -2 T, the series looks very
 197 similar after inversion of the momentum axis. The extrema
 198 occur symmetrically, at $q_s \approx -1.7 \mu\text{m}^{-1}$.

199 These observations are illustrated in Figs. 2(a) and 2(b),
 200 which present the energy and linewidth dispersions as a
 201 function of q , at $\varphi = \pi/4$, for both directions of the
 202 magnetic field. Since the linewidth η of the spin-wave
 203 Raman line yields the damping rate η_q of Eq. (1), Figs. 2(a)
 204 and 2(b) demonstrate that the SOC lifts the chiral degeneracy
 205 of the spin-wave energy as well as of the damping rate: the
 206 spin-wave energy and linewidth dispersions are both
 207 asymmetric and invariant under simultaneous inversion
 208 of the directions of the magnetic field and the wave
 209 vector.

210 Figure 1(e) shows a series of electronic Raman spectra
 211 obtained at $B = +2$ T, but for a different azimuthal angle
 212 $\varphi = 3\pi/4$. The momentum shift now changes to

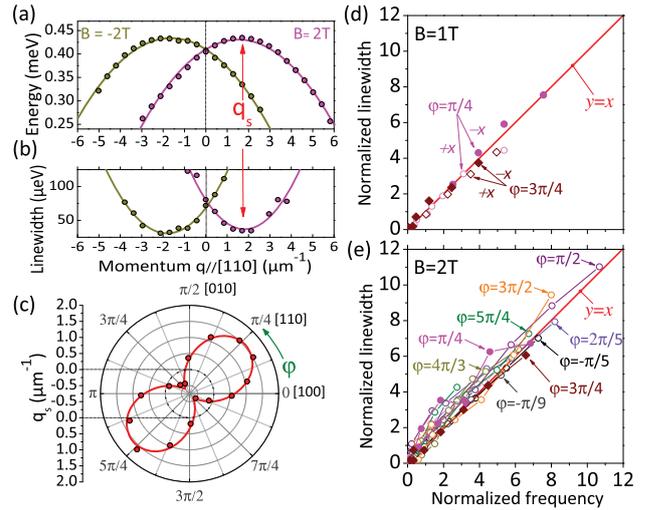


FIG. 2. [(a) and (b)] Lifting of the spin-wave chiral degeneracy
 by a momentum shift of the dispersions due to SOC: Momentum
 dispersion of energy (a) and linewidth (b) of the spin wave for
 $\varphi = \pi/4$ and $B = \pm 2$ T. Dispersions are shifted by q_s from $q = 0$
 with a mirror symmetry when inverting the magnetic field.
 (c) (circle) represents the q_s dependence with φ , which has been
 extracted from the dispersions measured for $\varphi \in [(-\pi/4), (3\pi/2)]$. The red curve is a fit of $q_s(\varphi)$ to the x
 component of $-\mathbf{q}_0$ given by Eq. (3). [(d) and (e)] Universal linear
 relation between the linewidth and the energy of the spin wave:
 $(\eta - \eta_0)/\eta_2$ is plotted as a function of $\frac{2m^*}{\hbar^2}(\hbar\omega - Z)/S_{\text{sw}}$; symbols
 of the same color are for a given in-plane angle φ , but for various
 values of q . (d) $B = +1$ T; open (solid) symbols correspond to
 spin waves with wave vector \mathbf{q} directed towards $-\mathbf{e}_x$ ($+\mathbf{e}_x$).
 (e) $B = +2$ T; solid symbols correspond, here, to the two
 extremal angles $\varphi = \pi/4, 3\pi/4$; open symbols are for other
 angles.

213 $q_s \approx -0.5 \mu\text{m}^{-1}$, which suggests a modulation of \mathbf{q}_s with
 214 φ . Indeed, Fig. 2(c) represents the experimental q_s
 215 extracted from the dispersions measured for various in-
 216 plane angles φ . q_s matches the \mathbf{e}_x component of $-\mathbf{q}_0$. The
 217 π -periodicity of the $q_s(\varphi)$ modulation is in complete
 218 agreement with the C_{2v} in-plane symmetry of the SOC
 219 arising from the superposition of the Rashba and
 220 Dresselhaus contributions and leading to the expression
 221 of \mathbf{q}_0 given in Eq. (3). Fitting the experimental values with
 222 Eq. (3) yields the Rashba and Dresselhaus constants α and
 223 β with high accuracy: we find $\alpha = 1.83 \pm 0.08 \text{ meV \AA}$ and
 224 $\beta = 3.79 \pm 0.11 \text{ meV \AA}$. To summarize, the quadratic
 225 energy and damping dispersions are both shifted by a \mathbf{q}_s
 226 modulated with φ , while the spin-wave stiffness $S_{\text{sw}} \approx$
 227 -27.5 ± 2.6 and damping $\eta_2 \approx 9.9 \pm 2.0 \text{ eV } \mu\text{m}^2$ remain
 228 protected.

229 Chirality in spin-wave energy dispersions and chiral
 230 damping has been observed in Fe monolayers [7]. Chiral
 231 damping dispersions have been observed in Pt/Co/Ni films
 232 [13]. However, Eqs. (1) and (5) show a universal linear
 233 relation between the damping rate and angular frequency of
 234 the spin wave, independent of SOC, which reads

$$\eta = \tilde{\eta}_0 + \frac{2m^*}{\hbar} \frac{\eta_2}{S_{\text{sw}}} \omega, \quad (6)$$

235 where ω stands for either ω_{sw} or $\omega_{\text{sw}}^{\text{SO}}$, and $\tilde{\eta}_0 =$
 236 $\eta_0 - 2mZ/\hbar^2 S_{\text{sw}}$. This universal linear behavior is demon-
 237 strated in Figs. 2(d) and 2(e) where the linewidth has been
 238 plotted as a function of energy for $B = +1 \text{ T}$ and $B = +2 \text{ T}$
 239 and various in-plane angles. The chirality and anisotropy do
 240 not appear anymore: $+\mathbf{e}_x$ and $-\mathbf{e}_x$ waves, for every φ , fall on
 241 the same line, which shows that the relation between spin-
 242 wave energy and damping does not depend on SOC but only
 243 on the Coulomb and kinetic interactions present in \hat{H}_0 . This
 244 confirms the existence of spin-orbit twisted spin waves
 245 predicted in Eq. (5). Moreover, the linear relation of
 246 Figs. 2(d) and 2(e) was not found in Ref. [13]. This
 247 unambiguously establishes the new physics underlying
 248 the spin-orbit twisted spin waves.

249 *Spin-wave group velocity control.*—We can now focus
 250 on the group velocity vector given by $\mathbf{v}_g = \nabla_{\mathbf{q}} \omega_{\text{sw}}$. In the
 251 absence of SOC, $\mathbf{v}_{g,\mathbf{q}} = S_{\text{sw}} \hbar \mathbf{q} / m^*$ is radial and vanishes at
 252 zero momentum. In the presence of SOC, Eq. (5) yields
 253 $\mathbf{v}_{g,\mathbf{q}} = S_{\text{sw}} \hbar (\mathbf{q} + \mathbf{q}_0) / m^*$. Except for $\varphi = \pi/4 (\text{mod } \pi/2)$,
 254 $\mathbf{v}_{g,\mathbf{q}}$ has acquired a nonradial component. The radial
 255 component vanishes along the $q = -q_{0x}$ curve. At
 256 $q = 0$, the group velocity is no longer 0 and depends on
 257 the respective directions of the magnetization and crystal-
 258 line axis: $\mathbf{v}_{g,q=0} = S_{\text{sw}} \hbar \mathbf{q}_0 / m^*$.

259 Since \mathbf{q}_0 depends on the magnetization direction and on
 260 the strength of the Rashba and Dresselhaus constants
 261 [Eq. (3)], the spin-orbit twist introduces a new way to
 262 control the spin-wave propagation direction, e.g., by varying
 263 the density by optical gating [18]. With this technique, the

264 electron density can be reproducibly reduced by up to a
 265 factor of 2 in our sample. We set $B = 2 \text{ T}$, and for each
 266 density we repeat the procedure exposed in Fig. 2 to extract
 267 the quantities S_{sw} , α , and β and evaluate the group velocity.
 268 Respective variations of the spin-wave stiffness, α and β ,
 269 with the density are given in Supplemental Material [18].

270 The group velocity control is summarized in Fig. 3, for
 271 the specific case of $\varphi = 3\pi/4$. The momentum shift \mathbf{q}_s (red
 272 dots) is plotted as it varies with the density $n_{2\text{D}}$. Standing
 273 spin waves correspond to the curve $q = q_s(n_{2\text{D}})$. When
 274 departing from this curve, the group velocity acquires a
 275 positive or negative component, which for that specific
 276 angle ($\varphi = 3\pi/4$) is always collinear with \mathbf{q} . For example,
 277 at fixed momentum transfer $q = -0.6 \mu\text{m}^{-1}$, the spin wave
 278 propagates upward when $n_{2\text{D}} = 2.7 \times 10^{11} \text{ cm}^{-2}$ and
 279 downward for $n_{2\text{D}} = 1.5 \times 10^{11} \text{ cm}^{-2}$. This illustrates the
 280 control of the spin-wave propagation direction that can be
 281 obtained via density control by optical gating (as shown
 282 here) or by electrical gating.

283 In conclusion, we showed that the interplay of SOC and
 284 Coulomb interaction in itinerant electronic systems pro-
 285 foundly affects the spin-wave dynamics. Our first-princi-
 286 ples predictions and related experimental confirmation
 287 demonstrate that, to leading order in the Rashba and
 288 Dresselhaus field strengths, the dispersions in energy
 289 and damping rate are both simply rigidly shifted by a
 290 wave vector \mathbf{q}_0 without any change of the universal relation
 291 between damping and energy. The rigid shift is similar to
 292 that of spin waves subject to Dzyaloshinskii-Moriya
 293 interaction (well suited for localized spins). However,
 294 the conservation of the universal relation is new. This

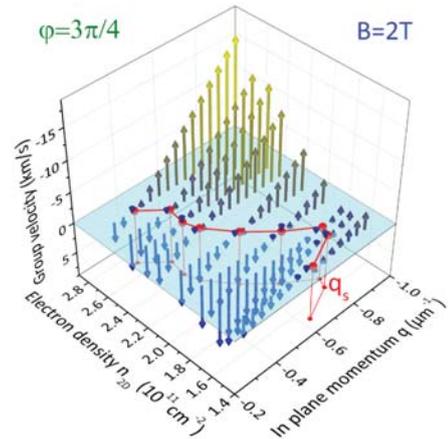


FIG. 3. Optical gating of the spin-wave group velocity. The
 group velocity vector changes for $\varphi = 3\pi/4$ and $B = 2 \text{ T}$ as
 a function of momentum and electron density (note that the group
 velocity is purely longitudinal at $\varphi = 3\pi/4$): a spin wave with
 momentum $q = -0.5 \mu\text{m}^{-1}$ experiences an inversion of its group
 velocity when the density is changed from 1.8 to
 $2.7 \times 10^{11} \text{ cm}^{-2}$. The red dots, where $q = q_s$, indicate a standing
 spin wave.

295 leads us to introduce the concept of spin-orbit twisted spin
 296 waves. Their group velocity acquires a nonradial compo-
 297 nent and can be controlled by the strength of the SOC. This
 298 effect opens up opportunities to control the propagation
 299 direction of spin waves by manipulating the SOC field
 300 strengths, e.g., by gating the sample. It can be exploited in
 301 spintronics to build, e.g., spin-wave routing devices or spin-
 302 wave lenses with patterning of the SOC.

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